



For exams in 2026 & onwards

INTRODUCTION TO ZUEB

The Ziauddin University Examination Board (ZUEB) is not only an awarding body but also a solution-driven educational organization dedicated to upholding the highest standards of academic excellence. ZUEB believes in Excellence, Integrity, and Innovation in Education. Established with a vision to foster a robust educational environment, ZUEB is committed to nurturing intellectual growth and development that meets international standards in an effective manner. The Ziauddin University Examination Board (ZUEB) was established through Government Gazette No. XLI on June 6th, 2018. Its purpose is to ensure a high quality, maintain global standards, and align the syllibi with national integrity within the examination system of Pakistan. ZUEB manages student appeals, regulates assessments, and reviews policies to maintain high standards.

WHY CHOOSE SSC-A AT ZUEB?

Ziauddin University Examination Board (ZUEB) offers the SSC-A (Secondary School Certificate advance) program, designed for students from international educational backgrounds. This program provides a structured, affordable, and academically strong pathway for learners to align with Pakistan's education system. It allows students to fulfil national curriculum requirements, including Urdu, Islamiyat, Pakistan Studies, or Sindhi, with academic integrity and flexible learning options. ZUEB believes no student should be left behind due to financial limitations or cross-system transitions, and SSC-A serves as a bridge between past efforts and future ambitions. It is the trusted choice for higher education in Pakistan.

SSC-ADVANCE MATHEMATICS

Mathematics in the SSC-advance qualification at ZUEB is a vital subject for students aspiring to excel in engineering, computer science, economics, and applied sciences. It develops essential skills in logical reasoning, abstract thinking, and quantitative problem-solving, which are critical for academic achievement and professional growth. By nurturing creativity in approaching mathematical challenges, the course equips learners with the intellectual tools required to succeed in both national and international examinations.

Aligned with national curriculum standards while also reflecting global academic expectations, SSC-A Mathematics offers a balanced and rigorous learning experience. Students engage with key areas such as algebra, geometry, trigonometry, calculus, probability, and statistics, delivered through a structured and supportive learning model that emphasizes both practice and application.

Whether your goal is to pursue engineering, data science, economics, or advance scientific research, SSC-A Mathematics provides a strong foundation to ensure you are academically prepared, nationally aligned, and globally competitive. Explore more on what SSC-A offers: ZUEB SSC-A Official Page.

	Syllabus Overview									
No.	Content	АО	Exam							
1	The Language of Mathematics	1,2,3	Combination of written exam papers (externally							
2	Algebra	1,2,3	set and marked)							
3	Graphs	1,2,3	Paper 1: Short Answer Questions							
4	Geometry	1,2,3	Duration: 1 hour 50 minutes							
5	Mensuration and Vectors	1,2,3	Paper 2: Structured Questions							
6	Probability and Statistics	1,2,3	Duration: 2 hours 10 minutes							

Description of Assessment Objectives

AO1 – Show knowledge and understanding of:

- scientific concepts and principles
- relevant methods, techniques, and procedures

AO2 – Apply knowledge and understanding to:

- use scientific ideas in various contexts
 perform and explain investigations, techniques, and procedures

AO3 - Analyse and interpret to:

- evaluate information and data
- draw reasoned conclusions and judgements
 suggest improvements to experimental methods

Weighting of Assessment Objectives

Assessment Objectives	P1 (%)	P2 (%)
A01	30	30
A02	40	40
A03	30	30

The Language of Mathematics

Aim: To introduce the foundational language that underpins most of mathematics.

	The learner will:	SLO#	Assessment Criteria - The learner can:	Cognitive levels
	The learner will.	3LO #	Assessment Citteria - The learner Can.	Cognitive levels
1	Understand integers, decimals and fractions.	1.1.1	Know and understand what an 'Integer' is, that they can be positive, negative or zero, and that they can be 'Odd' or 'Even'.	AO1
		1.1.2	Identify place values in integers and use them to interpret or construct numbers in expanded or positional form.	AO2
		1.1.3	Use a number line to place and order integers (positive, negative, and zero) in increasing or decreasing value.	AO2
		1.1.4	Use and interpret relational symbols $(=, \neq, <, >)$ and describe them in words (e.g., equal to, less than).	AO2
		1.1.5	Define and distinguish between proper fractions, improper fractions, and mixed numbers. (understanding proper and improper fractions is crucial for understanding mixed numbers)	AO1
		1.1.6	Know and Use standard mathematical notation to represent fractions and mixed numbers accurately.	AO2
		1.1.7	Know and identify the numerator and denominator of a fraction.	AO1
		1.1.8	Know and Understand the concept of equivalent fractions as having equal values despite different forms.	AO1
		1.1.9	Order a set of equivalent or unlike fractions by finding common denominators or using benchmarks on a number line.	AO3
2	Understand how to add, subtract, multiply and divide.	1.2.1	Know and Understand how to add, subtract, multiply, and divide positive and negative integers using written and mental strategies.	AO2
		1.2.2	Define and apply the terms 'product' and 'reciprocal' in arithmetic and algebraic contexts.	AO2
		1.2.3	Recognize that an operation is a mathematical process and describe examples of the four basic operations.	AO1
		1.2.4	Perform addition, subtraction, multiplication, and division with large whole numbers without the use of a calculator.	AO2
		1.2.5	Know and use 'inverse operation' and explain how it can be used to check or reverse a calculation.	AO2
		1.2.6	Know and use that addition and subtraction are inverse operations, and that multiplication and division are inverse operations.	AO2
3	Understand prime numbers	1.3.1	Know and Understand a prime number as an integer greater than 1 that has no positive factors other than 1 and itself.	AO1
		1.3.2	Recall and use the first six prime numbers (2, 3, 5, 7, 11, 13) in factorisation and divisibility tasks.	AO2
		1.3.3	Know and Understand that multiple of a number as the product of that number with an integer greater than 1.	AO1
		1.3.4	Know and Understand factors (or divisors) of a given integer.	AO1
		1.3.5	Know and use the Unique Prime Factorisation Theorem and its significance in number theory.	AO2
		1.3.6	Express integers as products of prime numbers, including exponential form.	AO2
		1.3.7	Identify and determine the Lowest Common Multiple (LCM) of two or more integers.	AO2
		1.3.8	Identify and determine the Highest Common Factor (HCF) of two or more integers.	AO2
		1.3.9	Use common factors and common multiples to simplify fractions and solve numerical problems.	AO3

4	Understand powers and roots.	1.4.1	Know and understand that a power represents repeated multiplication, and explain that squaring and cubing are powers of 2 and 3, respectively.	AO1
		1.4.2	Represent powers using indices notation (e.g., 2^3) and understand exponential form.	AO2
		1.4.3	Calculate the values of positive integer powers of numbers.	AO2
		1.4.4	Know and understand roots as inverse operations of powers, and distinguish between square roots and cube roots.	AO1
		1.4.5	Express roots using both root ($$) notation and fractional indices (e.g., N^(1/2) or N^(1/3).	AO2
		1.4.6	Calculate square and cube roots of numbers using exact or approximate methods.	AO2
		1.4.7	Demonstrate the inverse relationship between powers and roots (e.g., $\sqrt{N^2} = N$).	AO2
		1.4.8	Know and understand that not all roots result in integers and define a surd as an irrational root that cannot be simplified.	AO2
		1.4.9	Simplify numerical expressions involving square roots (e.g., $\sqrt{50}$ = $5\sqrt{2}$).	AO1
		1.4.10	Express results in exact form using fractions, surds, or powers of $\boldsymbol{\pi}$ unless approximation is required.	AO2
		1.4.11	Know and use the fact that the order of mathematical operations is clearly defined so that there is only one correct way of interpreting a sequence of written operations.	AO3
5	Understand fractions and ratios.	1.5.1	Know and understand that a vulgar (common) fraction is a fraction in which both the numerator and denominator are integers.	AO1
		1.5.2	Distinguish between proper and improper fractions based on their numerical value.	AO1
		1.5.3	Know and understand complex fractions as those in which the numerator and/or the denominator is itself a fraction.	AO1
		1.5.4	Simplify complex fractions, including through the division of fractions.	AO2
		1.5.5	Know and understand how to multiply proper, improper, and mixed fractions accurately.	AO2
		1.5.6	Know and use a fraction as a multiplicative inverse to solve problems.	AO2
		1.5.7	Simplify fractions by identifying and cancelling common factors in the numerator and denominator.	AO2
		1.5.8	Identify common multiples in denominators and use them to add or subtract fractions.	AO2
		1.5.9	Know and understand what a common denominator is, and explain its use in fraction operations.	AO1
		1.5.10	Simplify algebraic fractions where surds or powers appear in the numerator or denominator.	AO2
		1.5.11	Know and understand that a ratio is a comparison of two or more quantities and represent it using colon notation (a:b).	AO1
		1.5.12	Identify common multiples in denominators and use them to add or subtract fractions.	AO2
		1.5.13	Know and understand how ratios can be represented as fractions and vice versa.	AO2
		1.5.14	Use equal (equivalent) ratios to solve for unknown values in proportional reasoning tasks.	AO2
		1.5.15	Use ratios to solve problems involving real world contexts such as conversions, comparisons, scaling, mixing, and concentrations.	AO2
6	Understand decimals and percentages.	1.6.1	Know and understand that a decimal is a representation of a fractional (real) number.	AO1
		1.6.2	Distinguish between rational and irrational numbers by identifying which can or cannot be expressed as a ratio of integers.	AO3

	1.6.3	Identify and use place values accurately in decimal numbers.	AO2
•	1.6.4	Know and understand the difference between terminating and non-terminating decimals.	AO1
	1.6.5	Know and understand recurring decimals and represent them using dot notation (e.g., $0_{,2}$), ellipses, or overbars.	AO1
	1.6.6	Know and understand that all terminating and recurring decimals can be written as exact fractions, while other decimals are only approximations.	AO1
·	1.6.7	Convert between fractions and their equivalent decimals, and vice versa.	AO2
·	1.6.8	Know and understand that a percentage is a number out of 100 and explain its relationship to decimals and fractions.	AO1
·	1.6.9	Calculate the percentage of a given number.	AO2
·	1.6.10	Express one number as a percentage of another (e.g., 2 is 40% of 5).	AO2
·	1.6.11	Convert values between fractions, decimals, and percentages accurately.	AO2
·	1.6.12	Use percentages to compare quantities in real-life and mathematical contexts.	AO3
	1.6.13	Interpret and perform calculations with percentages greater than 100%.	AO3
	1.6.14	Solve problems involving percentage increase, decrease, and reverse percentage.	AO2
	1.6.15	Calculate repeated percentage change using successive multiplication of factors.	AO2
·	1.6.16	Apply the compound interest formula Total = P(1 + r/100)^n to solve real-life financial problems.	AO2
·	1.6.17	Recognize and express very large or very small numbers using standard form $A \times 10^n$, where $1 \le A < 10$ and n is an integer.	AO2
•	1.6.18	Use the laws of indices to simplify multiplication and division involving numbers in standard form.	AO2
Understand measurements and accuracy.	1.7.1	Demonstrate an understanding that all measurements involve an element of approximation, and explain how units, instruments, and context affect the precision and accuracy of a measurement.	AO2
·	1.7.2	Convert between standard and non-standard units of measurement using a given conversion factor.	AO2
·	1.7.3	Differentiate between decimal places and significant figures and round values accordingly to a specified level of accuracy.	AO2
·	1.7.4	Know and understand that a rounded value represents an interval and identify its possible range using the concepts of lower and upper bounds.	AO2
•	1.7.5	Calculate upper and lower bounds of a given rounded number and express the resulting interval using inequality notation (e.g., 2.35 ≤ x < 2.45).	AO2
·	1.7.6	Apply the concepts of upper and lower bounds in contextual problems involving measurement, area, or quantity.	AO2
•	1.7.7	Estimate the value of numerical expressions involving fractions, powers, or surds by applying appropriate rounding or truncation strategies.	AO3
		1.6.4 1.6.5 1.6.6 1.6.7 1.6.8 1.6.9 1.6.10 1.6.11 1.6.12 1.6.13 1.6.14 1.6.15 1.6.16 1.6.17 1.6.18 Understand measurements and accuracy. 1.7.1 1.7.2 1.7.3 1.7.4 1.7.5 1.7.6	1.6.4 Know and understand the difference between terminating and non-terminating decimals. 1.6.5 Now and understand recurring decimals and represent them using dot notation (e.g., 3), ellipses, or overbars. 1.6.6 Know and understand that all terminating and recurring decimals can be written as exact fractions, while other decimals are only approximations. 1.6.7 Convert between fractions and their equivalent decimals, and vice versa. 1.6.8 Know and understand that a percentage is a number out of 100 and explain its relationship to decimals and fractions. 1.6.9 Calculate the percentage of a given number. 1.6.10 Express one number as a percentage of another (e.g., 2 is 40% of 5). 1.6.11 Convert values between fractions, decimals, and percentages accurately. 1.6.12 Use percentages to compare quantities in real-life and mathematical contexts. 1.6.13 Interpret and perform calculations with percentages greater than 100%. 1.6.14 Solve problems involving percentage increase, decrease, and reverse percentage. 1.6.15 Calculate repeated percentage change using successive multiplication of factors. Apply the compound interest formula Total = P(1 + r/100)*n to solve real-life financial problems. 1.6.16 Apply the compound interest formula Total = P(1 + r/100)*n to solve real-life financial problems. 1.6.17 Use the two of indices to simplify multiplication and division involving numbers in standard form. 1.6.18 Use the two of indices to simplify multiplication and division involving numbers in standard form. 1.7.1 Sometistae in understanding that all measurements involve an element of approximation, and explain how units, instruments, and context affect the precision and accuracy. 1.7.2 Convert between decimal places and significant figures and round values accordingly to a specified level of accuracy. 1.7.3 Differentiate between decimal places and significant figures and round values accordingly to a specified level of accuracy. 1.7.4 Know and understand that a rounded value represents an interval and iden

Algebra

Aim: To turn mathematical problems into equations with unknown values in them, and manipulate those equations to solve real-world problems.

	The learner will:	SLO#	Assessment Criteria - The learner can:	Cognitive levels
1	Understand the language of algebra.	2.1.1	Know and understand that a variable is a number that can take different values in an expression or equation.	AO1
		2.1.2	Know and understand that symbols can be used to represent unknown values or changing quantities in mathematical contexts.	AO1
		2.1.3	Know and understand that an expression is a mathematical statement consisting of numbers, variables, and operators without an equality or inequality.	AO1
		2.1.4	Know and understand that a formula is a mathematical rule or relationship that connects two or more quantities using algebraic expressions.	AO1
		2.1.5	Know and understand that an equation is a formula that states two expressions are equal in value.	AO1
		2.1.6	Use and interpret relational symbols ≤ (less than or equal to) and ≥ (greater than or equal to), and describe their meaning in written and symbolic form.	AO2
		2.1.7	Know and understand that an inequality is a statement comparing two expressions using <, >, ≤, or ≥.	AO1
		2.1.8	Know and understand that an identity is an equation that is always true for all values of the variable.	AO1
		2.1.9	Know and understand that a term is a part of an algebraic expression separated by + or – signs.	AO1
		2.1.10	Know and understand that a factor is a quantity that multiplies another quantity in an expression or equation.	AO1
		2.1.11	Know and understand that algebraic expressions follow the standard rules of arithmetic: commutativity, associativity, and distributivity.	AO1
2	Understand the notations used to make algebra easier to write.	2.2.1	Use standard algebraic notation to represent multiplication and division, such as; • a b instead of a × b , • $3a$ instead of a + a + a , or 3 × a • a^2b instead of a × a × b , • a $/b$ instead of a ÷ b , • a $/b$ instead of 1.5 a .	AO2
		2.2.2	Use brackets to group terms in algebraic expressions and recognize their effect on order of operations.	AO2
		2.2.3	Use and interpret index notation for positive or negative, integer, fractional or zero powers: $a\times a\times a\equiv a^3$ $\frac{1}{a^3}\equiv a^{-3}$ $a^0\equiv \frac{1}{a^0}\equiv 1$ $\sqrt[3]{a^2}\equiv a^{\frac{2}{3}}$ $\frac{1}{\sqrt{a}}\equiv a^{-\frac{1}{2}}$	AO2
		2.2.4	Know and use the index laws to simplify expressions: $x^m \times x^n \equiv x^{m+n}$ $x^m \div x^n \equiv x^{m-n}$ $(x^m)^n \equiv x^{mn}$	AO2
		2.2.5	Evaluate algebraic expressions by substituting values for variables and calculating the result.	AO2
		2.2.6	Know and understand that a 'Linear' expression is one where variables appear with a maximum power of 1 and identify such expressions in algebraic form.	AO1
		2.2.7	Know and understand that a 'Quadratic' expression is one that contains at least one variable, and the terms with the highest power are of the form $x = 2$ and/or $x = y = 1$.	AO1

3	Understand how to simplify and manipulate algebraic expressions.	2.3.1	Know and understand that "simplify" is the process of rewriting an expression in a less complicated or more efficient form using fewer terms or simpler structures.	AO2
		2.3.2	Simplify expressions by collecting like terms.	AO2
		2.3.3	Simplify expressions by factoring out a common numerical or algebraic factor.	AO2
		2.3.4	Simplify expressions by cancelling identical terms in numerators and denominators or across equations.	AO2
		2.3.5	Simplify expressions by cancelling factors when they appear in both the numerator and denominator of algebraic fractions.	AO2
		2.3.6	Simplify algebraic fractions where numerators and/or denominators are numeric, linear, or quadratic.	AO2
		2.3.7	Apply the laws of indices to simplify expressions involving powers and variables.	AO3
		2.3.8	Factorize quadratic expressions in the general form ($a \ x^2 + b \ x + c$), including the difference of squares pattern.	AO2
		2.3.9	Rewrite quadratic expressions in completed square form.	AO2
4	Understand how to manipulate algebraic expressions to solve	2.4.1	Expand single brackets by multiplying a term across the bracket.	AO2
	problems.	2.4.2	Expand binomial expressions by multiplying two brackets.	AO3
		2.4.3	Manipulate algebraic fractions with linear or quadratic numerators and denominators through simplification and rewriting.	AO3
		2.4.4	Use algebraic manipulation and simplification to prove that two expressions are equivalent.	AO3
		2.4.5	Know and understand that a function is a rule that assigns each input exactly one output, and represent it using algebraic expressions.	AO1
		2.4.6	Know and understand the inverse of a function as the operation that reverses the effect of the original function.	AO1
		2.4.7	Know and understand direct proportion as a relationship between two variables in the form .	AO1
		2.4.8	Manipulate simple linear or rational equations to find the inverse function algebraically.	AO3
		2.4.9	Know and understand that a composite function is one where the output of one function is used as the input of another (notation not required).	AO1
		2.4.10	Apply algebraic techniques such as expansion, simplification, and substitution to justify conclusions and construct mathematical proofs.	AO3
5	Understand how to solve equations and inequalities.	2.5.1	Know and understand that 'solving' an equation is finding all values of the unknown variable that make the equation true.	AO1
		2.5.2	Substitute numerical values into algebraic expressions and formulas to calculate results.	AO2
		2.5.3	Solve linear equations in one variable, including those with the unknown on both sides.	AO2
		2.5.4	Know and understand that quadratic equations may have zero, one, or two real solutions.	AO1
		2.5.5	Use the 'Quadratic Formula', $x=\frac{-b\pm\sqrt{b^2-4ac}}{2a}$, to obtain the solutions to a quadratic equation of the	AO2
			form $a x^2 + b x + c = 0$ (equation given).	
		2.5.6	Solve quadratic equations by rearranging, factorising, completing the square, or applying the quadratic formula.	AO3

		2.5.7	Know and understand that simultaneous equations are equations with shared unknowns and explain that their solutions satisfy all equations in the system.	AO1
		2.5.8	Solve simultaneous equations where both are linear, or one is linear and the other quadratic.	AO3
		2.5.9	Rearrange equations into iterative form suitable for approximation methods.	AO2
		2.5.10	Use iteration to find approximate numerical solutions to equations, given a starting value.	AO2
		2.5.11	Formulate linear, quadratic, or simultaneous equations from written problems, solve them, and interpret the results in context.	AO3
		2.5.12	Express exponential growth or decay problems using iterative models (e.g., compound interest formulas).	AO3
		2.5.13	Solve and interpret real-life growth and decay problems mathematically.	AO3
6	Understand sequences.	2.6.1	Know and understand that a sequence is an ordered list of numbers generated by a specific rule or function.	AO1
		2.6.2	Distinguish between term-to-term rules and position-to-term rules used to define sequences.	AO3
		2.6.3	Apply the rule of a given sequence to find specified terms.	AO2
		2.6.4	Know and understand arithmetic sequences and identify the common difference as the fixed interval between consecutive terms.	AO1
		2.6.5	Know and use the fact that the nth term of an arithmetic sequence is given by $x_n = a + d(n - 1)$ where a is the first term and d is the common difference.	AO2
		2.6.6	Derive the nth term formula of an arithmetic sequence.	AO3
		2.6.7	Know and understand geometric sequences and define the common ratio as the factor by which each term is multiplied to get the next.	AO1
		2.6.8	Use the formula for the nth term of a geometric sequence, first term and r is the common ratio (r > 0, rational or surd). $x_n = ar^n$ where a is the	AO2
		2.6.9	Know and understand that the triangular number sequence is one where objects can form equilateral triangles.	AO1
		2.6.10	Use the nth term formula for the triangular number sequence $x_{ m n}=rac{n(n+1)}{2}$	AO2
		2.6.11	Know and understand the square number sequence and express it with the nth term formula $x_n = n^2$.	AO1
		2.6.12	Know and understand the cubic number sequence and express it with the nth term formula $x_n = n^{-3}$.	AO1
		2.6.13	Know and understand that the 'Fibonacci Sequence' is the sequence where the nth term is the sum of the previous two terms , $x_n = x_{n-1} + x_{n-2}$ and that the sequence is defined as starting [0, 1, 1,].	AO1
		2.6.14	Know and understand a quadratic sequence as one in which the second difference between terms is constant.	AO1
		2.6.15	Know and use the nth term formula for quadratic sequences $x_n = ax^2 + bx + c$	AO2

Graphs

Aim: To draw/plot accurate graphs from data sets or functions, and use them to extract additional data.

	The learner will:	SLO#	Assessment Criteria - The learner can:	Cognitive levels
1	Understand how to draw graphs.	3.1.1	Draw horizontal and vertical axes using a ruler with precision and neatness.	AO2
		3.1.2	Label axes with appropriate variable names and include units of measurement where relevant.	AO2
		3.1.3	Apply correct scale to axes using increments of 1, 2, or 5; clearly label starting values if the scale does not begin at zero.	AO2
		3.1.4	Plot individual data points using crosses, ensuring that the center of the cross lies within half a square of the intended location.	AO2
		3.1.5	Draw a straight line of best fit for a linear data set using a ruler.	AO2
		3.1.6	Label each data set clearly when multiple sets are plotted on the same set of axes.	AO2
		3.1.7	Construct a gradient triangle that is at least half the height or width of the graph to calculate or represent gradient visually.	AO3
		3.1.8	Shade the region under a graph when required to represent area.	AO2
		3.1.9	Draw sketch graph axes with a ruler to represent general trends or function shapes.	AO2
		3.1.10	Label sketch graph axes with variable names but omit units to distinguish from measured data.	AO2
		3.1.11	Sketch the general shape of curves or graphs based on their algebraic form or qualitative trend.	AO3
2	Understand how to plot linear graphs in cartesian coordinates.	3.2.1	Know and use the Cartesian coordinate system to describe and locate points in two-dimensional space.	AO1
		3.2.2	Plot points and graphs using all four quadrants of the Cartesian plane.	AO2
		3.2.3	Identify the coordinates of given points on a graph and describe their positions accurately.	AO2
		3.2.4	Calculate the midpoint of a straight line segment given the coordinates of its endpoints.	AO2
		3.2.5	Recognize and apply the general form of a straight-line equation; $y = m x + c$.	AO2
		3.2.6	Identify graphs showing direct proportionality as straight lines through the origin in the form; $y = mx$.	AO3
		3.2.7	Determine the equations for horizontal lines, vertical lines, and diagonal lines that pass through the origin.	AO3
		3.2.8	Determine whether two lines are parallel or perpendicular by analyzing their gradients.	AO3
		3.2.9	Construct the equation of a straight line given either: (a) two points it passes through or (b) one point and its gradient.	AO3
		3.2.10	Plot straight-line graphs using their algebraic equations.	AO2

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		3.2.11	Determine the gradient (m) and y-intercept (c) from a linear graph, and interpret these in context where applicable.	AO3
3	Understand graphs of functions.	3.3.1	Plot and sketch graphs of quadratic and simple cubic functions involving up to three terms.	AO2
		3.3.2	Plot and sketch graphs of the reciprocal function $y = \frac{1}{x} v hen x \neq 0$, and exponential functions of the form $y = k^x$ where k is positive.	AO2
		3.3.3	Sketch the graphs of the trigonometric functions, and, for θ measured in degrees.	AO2
		3.3.4	Apply and sketch transformations of functions including vertical and horizontal translations, 1-D stretches, and reflections in the x-axis, y-axis, or line .	AO3
		3.3.5	Use graphs to determine the value(s) of x for a given y-value, or vice versa.	AO2
		3.3.6	Identify key features on function graphs such as roots (x-intercepts), y-intercepts, and turning points.	AO3
		3.3.7	Determine graphically the point(s) of intersection between two graphs, including cases with one linear and one non-linear function.	AO3
		3.3.8	Know and use the fact that the intersection of two graphs represents the solution to the equation $f_1(x) - f_2(x) = 0$.	AO3
		3.3.9	Recall and apply the equation of a circle centred at the origin; $x^2 + y^2 = r^2$	AO2
		3.3.10	Draw the graph of a circle given its equation in standard form.	AO2
		3.3.11	Determine the equation of a circle centred at the origin from its graphical representation.	AO3
		3.3.12	Determine the equation of the tangent to a circle at a given point using geometric or algebraic reasoning.	AO3
		3.3.13	Use graphs to approximate the solutions to equations, including axis intercepts (roots) and points of intersection for simultaneous equations.	AO3
		3.3.14	Graph linear inequalities in one or two variables, and quadratic inequalities in one variable, using solid lines ≥ and ≤, and dashed lines for < and >.	AO3
4	Understand gradients.	3.4.1	Calculate the gradient of a straight-line graph and estimate the area under it using box counting or polygonal methods.	AO2
		3.4.2	Estimate the gradient at a point and the area under a non-linear graph using approximation strategies such as tangents and numerical methods.	AO3
		3.4.3	Solve problems using gradient and area from graphs in both mathematical and real-life contexts.	AO3
		3.4.4	Interpret the gradient of a straight line as the rate of change of a function or relationship.	AO3
		3.4.5	Interpret the gradient at a specific point on a curve as the instantaneous rate of change.	AO3
		3.4.6	Estimate the average rate of change over an interval by approximating the curve with a straight line and calculating its gradient.	AO3
		3.4.7	Determine both average and instantaneous rates of change from chords and tangents using numerical, algebraic, or graphical techniques.	AO3
		3.4.8	Recognize that if x is inversely proportional to y, then the relationship is represented by the equation.	AO2
		3.4.9	Plot x against for inverse proportionality and interpret the gradient of the graph as the constant of proportionality.	AO3
		3.4.10	Interpret and extract information from real-life graphs including distance-time, velocity-time, and financial graphs (e.g., profit vs. time).	AO3
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Geometry

Aim: To analyse and draw shapes in two and three dimensions.

	The learner will:	SLO#	Assessment Criteria - The learner can:	Cognitive levels
1	Understand the language of geometry.	4.1.1	Know and understand that a dimension is a measure of extent in a single direction, and use the terms 1-D, 2-D, and 3-D to describe the number of dimensions an object occupies.	AO2
		4.1.2	Know and understand that a point is an exact location with no size or dimension.	AO1
		4.1.3	Know and understand that a straight line is an infinite 1-dimensional set of points extending in both directions.	AO1
		4.1.4	Know and understand that segment is a finite part of a line with two endpoints and measurable length.	AO1
		4.1.5	Know and understand that an edge is a line segment that forms part of the boundary of a 2-D shape.	AO1
		4.1.6	Know and understand that a vertex is a point where two or more edges meet.	AO1
		4.1.7	Know and understand a plane is a flat, two-dimensional surface that extends infinitely in all directions.	AO1
		4.1.8	Know and understand that a polygon is a closed 2-D shape formed by at least three straight edges.	AO1
		4.1.9	Distinguish between regular polygons (equal sides and angles) and irregular polygons.	AO2
		4.1.10	Name and identify polygons with 3 to 10 sides: Triangle, Quadrilateral, Pentagon, Hexagon, Heptagon, Octagon, Nonagon, and Decagon.	AO1
		4.1.11	Know and understan d parallel lines as lines that are always the same distance apart and never intersect.	AO1
		4.1.12	Know and understand a right angle as a 90° angle, typically marked with a square corner.	AO1
		4.1.13	Know and understand that perpendicular lines are lines that intersect at a right angle.	AO1
		4.1.14	Know and understand a perpendicular bisector as a line that crosses a line segment at its midpoint and at a 90° angle.	AO2
		4.1.15	Know and use the geometric naming convention to describe points, line segments, and angles (e.g., point A, segment AB, angle ∠ABC).	AO2
		4.1.16	Know and understand that perimeter is the total length around the boundary of a polygon, and calculate it by summing the side lengths.	AO1

2	Understand angles between lines.	4.2.1	Know and use the fact that the sum of the angles on a straight line is 180°.	AO2
		4.2.2	Know and use the fact that the sum of the angles around a point is 360°.	AO2
		4.2.3	Know and understand that when a line crosses two parallel lines, the resulting angles fall into three categories: alternate, allied, and corresponding angles.	AO1
		4.2.4	Know and understand that alternate angles are equal and describe their 'Z-shape' pattern when a transversal cuts the two parallel lines.	AO1
		4.2.5	Know and understand that allied (or co-interior) angles are supplementary (add to 180°), and describe their "C-shape" or "U-shape" pattern.	AO1
		4.2.6	Know and understand that the corresponding angles are equal and describe their 'F-shape' pattern.	AO1
		4.2.7	Use alternate, allied, and corresponding angle rules to calculate unknown angles in diagrams with parallel lines.	AO2
		4.2.8	Know and understand interior angles as angles inside a polygon and exterior angles as angles between one side and the extension of an adjacent side.	AO1
		4.2.9	Know and understand the rule that an interior angle and its adjacent exterior angle form a linear pair (sum to 180°).	AO1
		4.2.10	Know and understand the fact that the interior angles of a triangle add up to 180°.	AO1
		4.2.11	Determine the sum of interior angles in any polygon by dividing the shape into triangles.	AO3
		4.2.12	Know and use the fact that the exterior angle of a triangle equals the sum of the two opposite interior angles.	AO2
		4.2.13	 Know and use the formulas: Sum of interior angles of an n-sided polygon = (n-2) x 180 degrees Sum of exterior angles of any polygon = 360° 	AO2
		4.2.14	Determine the interior and exterior angles of a regular polygon.	AO3
		4.2.15	Determine unknown angles in diagrams using all known angle rules and properties.	AO3
3	Understand triangles.	4.3.1	Know and understand an equilateral triangle as a regular triangle with all sides and angles equal.	AO1
		4.3.2	Know and understand that an isosceles triangle is a triangle with two equal sides and two equal angles.	AO1
		4.3.3	Know and understand that a right-angled triangle is one that contains a 90° angle.	AO1
		4.3.4	Know and understand that the sides of a right-angled triangle are: hypotenuse (the longest side opposite the right angle), opposite (relative to a given non-right angle), and adjacent (the remaining side next to the given angle).	AO1
		4.3.5	Know and understand Pythagoras' Theorem $a^2 + b^2 = c^2$ to find missing side lengths in right-angled triangles.	AO1

		4.3.6	Know and understand that a scalene triangle is one with no equal sides or angles.	AO1
		4.3.7	Know and use the standard triangle naming convention where each side, angle, and vertex are represented by corresponding letters (e.g., side AB opposite angle C).	AO2
4	Understand quadrilaterals.	4.4.1	Know and understand that square is a quadrilateral with four equal sides and four right angles.	AO1
		4.4.2	Know and use the fact that in a square, opposite sides are parallel and diagonals bisect each other at right angles.	AO2
		4.4.3	Know and understand that a rectangle is a quadrilateral with four right angles and two pairs of equal opposite sides.	AO1
		4.4.4	Know and use the fact that in a rectangle, opposite sides are parallel, diagonals bisect each other, and every square is also a rectangle.	AO2
		4.4.5	Know and understand that a parallelogram is a quadrilateral with opposite sides equal in length and opposite angles equal in size.	AO1
		4.4.6	Know and use the fact that in a parallelogram, opposite sides are parallel, diagonals bisect each other, and every rectangle is a parallelogram.	AO2
		4.4.7	Know and understand that a rhombus is a quadrilateral with four equal sides and equal opposite angles.	AO1
		4.4.8	Know and use the fact that in a rhombus, opposite sides are parallel, diagonals bisect each other at right angles, all squares are rhombuses, and all rhombuses are parallelograms.	AO2
		4.4.9	Know and understand that a trapezium is a quadrilateral with exactly one pair of parallel sides.	AO1
		4.4.10	Know and use the fact that every parallelogram meets the definition of a trapezium.	AO2
		4.4.11	Know and understand that a kite is a quadrilateral with two distinct pairs of adjacent equal sides.	AO1
		4.4.12	Know and use the fact that in a kite, diagonals bisect each other at right angles, and that all rhombuses are kites.	AO2
5	Understand circles.	4.5.1	Know and understand that a circle is the set of all points that are a fixed distance from a central point, called the centre.	AO1
		4.5.2	Know and understand that the radius is the distance from the centre of the circle to any point on the circle.	AO1
		4.5.3	Know and understand that the diameter is a line segment that passes through the centre and has endpoints on the circle; understand that the diameter is twice the radius.	AO1
		4.5.4	Know and understand that the circumference is the perimeter or total distance around a circle.	AO1
		4.5.5	Know and understand that a chord is a line segment with both endpoints on the circle, not necessarily passing through the centre.	AO1
		4.5.6	Know and understand that a tangent is a line that touches the circle at exactly one point.	AO1

	4.5.7	Know and understand that an arc is a continuous portion of the circle's circumference between two points.	AO1
	4.5.8	Know and understand that a sector is the area bounded by two radii and the arc between them; identify the major sector as the larger region and the minor sector as the smaller.	AO1
	4.5.9	Know and understand that a segment is the area bounded by a chord and the arc connecting its endpoints; identify the major segment as the larger region and the minor segment as the smaller.	AO1
Understand the circle theorems.	4.6.1	Know and use the fact that a tangent to a circle is perpendicular (90°) to the radius at the point where it touches the circle.	AO2
	4.6.2	Know and use the fact that two radii and the chord joining their endpoints form an isosceles triangle.	AO2
	4.6.3	Know and use the fact that the perpendicular bisector of any chord passes through the centre of the circle.	AO2
	4.6.4	Know and use the fact that the angle at the centre of a circle is twice the angle at the circumference when both angles subtend the same arc.	AO2
	4.6.5	Know and use the fact that a triangle formed by a diameter and a point on the circle always has a right angle opposite the diameter.	AO2
	4.6.6	Know and use the fact that angles formed in the same segment (from the same chord) are equal, and that the angle in the major and minor segment always adds to 180°.	AO2
	4.6.7	Know and use the fact that opposite angles in a cyclic quadrilateral (where all vertices lie on the circle) always add up to 180°.	AO2
	4.6.8	Know and use the fact that the lengths of two tangents drawn from a point outside a circle to the circle are equal.	AO2
	4.6.9	Know and use the fact that the angle between a tangent and a chord is equal to the angle in the alternate segment of the circle.	AO2
	4.6.10	Apply known circle theorems (by name or description) to explain geometric relationships and solve problems involving angles and lengths in diagrams.	AO2
Jnderstand congruent and similar shapes.	4.7.1	Know and use the fact that congruent shapes are shapes that are exactly the same in size and shape but may differ in orientation due to rotation or reflection.	AO2
	4.7.2	Know and use the triangle congruence using the rules; o SSS (Side-Side-Side) o AAS (Angle-Angle-Side) o SAS (Side-Angle-Side) o RHS (Right angle—Hypotenuse—Side) and use these criteria in geometric arguments.	AO2
	4.7.3	Know and use the fact that similar shapes as shapes that have the same form but may differ in size due to enlargement, rotation, or reflection.	AO2
	4.7.4	Know and use the fact that triangle similarity can be established by using the following rules: o Two corresponding angles are equal o All corresponding sides are proportional o Two sides are proportional and the angle between them is equal	AO2
	4.7.5	Use ratio and proportion to calculate unknown side lengths in similar shapes.	AO2
	4.7.6	Recognize and distinguish between congruent and similar figures in diagrams.	AO3
J	theorems.	4.5.8 4.5.9 Understand the circle theorems. 4.6.1 4.6.2 4.6.3 4.6.4 4.6.5 4.6.6 4.6.7 4.6.8 4.6.9 4.6.10 Anderstand congruent and similar shapes. 4.7.1 4.7.2	Know and use the fact that the perpendicular bisector of any chord passes through the centre of the circle the circle the circle the circle. Know and use the fact that two radii and the chord joining their endpoints form an isosceles triangle. Know and use the fact that two radii and the chord joining their endpoints form an isosceles triangle. Know and use the fact that two radii and the chord joining their endpoints form an isosceles triangle. Know and use the fact that two radii and the chord joining their endpoints form an isosceles triangle. Know and use the fact that two radii and the chord joining their endpoints form an isosceles triangle. Know and use the fact that the angle at the centre of a circle is twice the angle at the circumference when both angles subtend the same arc. Know and use the fact that the angle at the centre of a circle is twice the angle at the circumference when both angles subtend the same arc. Know and use the fact that a triangle formed by a diameter and a point on the circle always has a right angle opposite the diameter. Know and use the fact that a triangle formed by a diameter and a point on the circle always has a right angle opposite the diameter. Know and use the fact that a pagle in the major and minor segment (from the same chord) are equal, and that the angle in the major and minor segment always add to 180°. Know and use the fact that the lengths of two tangents drawn from a point outside a circle to the circle) always add up to 180°. Know and use the fact that the angle between a tangent and a chord is equal to the angle in the alternate segment of the circle. 4.6.10 Apply known circle theorems (by name or description) to explain geometric relationships and solve problems involving angles and lengths in diagrams. Know and use the fact that to ongruent shapes are shapes that are exactly the same in size and shape but may differ in orientation due to rotation or reflection. Know and use the fact that timagle congruence using the rules; 2.5.8 (Side-Angl

		4.7.7	Apply the properties of congruent and similar shapes to complete or explain simple geometric proofs.	AO2
		4.7.8	Know and use the fact that line symmetry and rotational symmetry in 2-D shapes.	AO2
		4.7.9	State the number of lines of symmetry in a given polygon.	AO3
		4.7.10	Accurately draw all lines of symmetry for a polygon.	AO2
		4.7.11	State the order of rotational symmetry of a polygon.	AO2
		4.7.12	Know and understand that a shape with no rotational symmetry has an order of 1.	AO1
8	Understand construction methods.	4.8.1	Know and understand how to use a ruler, compass, and protractor accurately to construct geometric shapes and diagrams; show all construction lines clearly.	AO1
		4.8.2	Know and understand that a locus is a set of points that satisfy a given condition (e.g., a fixed distance from a point or line).	AO1
		4.8.3	Construct loci accurately using appropriate tools, showing all construction lines.	AO2
		4.8.4	Construct triangles using ruler and compass, or ruler and protractor, given sides and/or angles.	AO2
		4.8.5	Construct the locus of points at a fixed distance from a single point (a circle).	AO2
		4.8.6	Construct the angle bisector as the locus of points equidistant from two intersecting lines.	AO2
		4.8.7	Construct the perpendicular bisector of a line segment as the locus of points equidistant from two endpoints	AO2
		4.8.8	Construct a line perpendicular to another line through a given point.	AO2
		4.8.9	Construct accurate angles of 60° and 90° using compass and straightedge.	AO2
		4.8.10	Construct the locus of points at a fixed distance from a straight line (parallel lines).	AO2
		4.8.11	Construct the locus of points at a fixed distance from a line segment (capsule shape).	AO2
		4.8.12	Draw regions satisfying a set of given geometric constraints using construction techniques.	AO2
		4.8.13	Know and understand the fact that the shortest distance from a point to a line is measured along the perpendicular.	AO1
		4.8.14	Use construction to demonstrate that the perpendicular line represents the shortest distance from a point to a line.	AO2

	4.8.15	Interpret written geometric descriptions and produce accurate diagrams using construction tools.	AO3
Understand transformations.	4.9.1	Know and understand that a translation is a movement in a straight line, represented by a vector, and apply translations to geometric shapes by shifting each vertex.	AO1
	4.9.2	Draw the image of a shape after translation using a given vector.	AO2
	4.9.3	Know and understand that a rotation is a circular movement around a fixed point (centre of rotation), described by angle, direction, and centre.	AO1
	4.9.4	Draw rotations of 90°, 180°, or 270° clockwise or anti-clockwise about a given point.	AO2
	4.9.5	Know and understand that a reflection is a flip over a line of symmetry, described by the equation of the reflection line (e.g.,y=x).	AO1
	4.9.6	Draw reflections of shapes in the x-axis, y-axis, and the line.	AO2
	4.9.7	Identify single transformations that leave a shape unchanged in appearance.	AO3
	4.9.8	Describe how a shape changes under combinations of transformations and relate the outcome to the original position.	AO3
	4.9.9	Know and understand that an enlargement is a transformation that changes the size of a shape about a centre, described using a scale factor and centre of enlargement.	AO1
	4.9.10	Interpret the scale factor of an enlargement: Scale factor > 1 enlarges Scale factor < 1 reduces Negative scale factor produces an image on the opposite side of the centre, rotated 180°.	AO3
	4.9.11	Draw enlargements of geometric shapes with scale factors such as 4, 3, 2, $\frac{1}{2}$, $\frac{1}{3}$, and $\frac{1}{4}$ (positive or negative).	AO2
	4.9.12	Know and understand how scale factor affects dimensions: Lengths change by scale factor Areas change by the square of the scale factor Volumes change by the cube of the scale factor	AO1
	4.9.13	Use scale factors to interpret and extract information from scale diagrams and maps.	AO2
Understand 3D shapes.	4.10.1	Know and understand that a cube is a 3D shape with six square faces, equal edge lengths, and right angles between all faces.	AO1
	4.10.2	Know and understand that a cuboid is a 3D shape with six rectangular faces and all internal angles equal to 90°.	AO1
	4.10.3	Know and understand that a tetrahedron is a 3D shape with four triangular faces.	AO1
	4.10.4	Know and understand that a square-based pyramid is a 3D shape with one square face and four isosceles triangular faces meeting at a vertex.	AO1
	4.10.5	Know and understand a right prism is a 3D shape with a constant cross-section (e.g., cylinder, triangular prism).	AO1
	4.10.6	Know and understand that a sphere is a 3D shape with a surface that is always the same distance (radius) from a central point.	AO1
	transformations.	Understand transformations. 4.9.1 4.9.2 4.9.3 4.9.4 4.9.5 4.9.6 4.9.7 4.9.8 4.9.9 4.9.10 4.9.11 4.9.12 4.9.13 Understand 3D shapes. 4.10.1 4.10.2 4.10.3 4.10.4 4.10.5	Understand transformations. 4.9.1 by a vaccior, and apply translation is a movement in a straight line, represented by a vaccior, and apply translations to geometric shapes by shifting each vertex. 4.9.2 braw the image of a shape after translation using a given vector. 4.9.3 Know and understand that a rotation is a circular movement around a fixed point (centre of rotation), described by angle, direction, and centre. 4.9.4 braw rotations of 90°, 180°, or 270° clockwise or anti-clockwise about a given point. 4.9.5 Know and understand that a reflection is a flip over a line of symmetry, described by the equation of the reflection line (e.g., y=x.). 4.9.6 braw reflections of shapes in the x-axis, y-axis, and the line. 4.9.7 Identify single transformations that leave a shape unchanged in appearance. 4.9.8 bescribe how a shape changes under combinations of transformations and relate the outcome to the driginal position. 4.9.9 Know and understand that an enlargement is a transformation that changes the size of a shape about a centre, described using a scale factor and centre of enlargement. 5. Stale factor 1 enlarges. 5. Stale factor 2 to enlarges. 5. Stale factor 3 to enlarge and 1 enlargement. 5. Stale factor 4 reduces. 5. Stale factor 5 to enlarges. 6. Stale factor 5 to enlarges. 6. Stale factor 5 to enlarges. 7. Stale factor 6 to engative). Know and understand how scale factor and provides an image on the opposite side of the centre, rotated 180°. 8. Now and understand how scale factor and factor scale factor. 9. Volumes change by the equare of the scale factor. 9. Volumes change by the cuter of the scale factor. 9. Volumes change by the cuter of the scale factor. 1.0.1 Know and understand that a cuboid is a 3D shape with six sequare faces, equal edge lengths, and right angles equal to 90°. 1.10.1 Know and understand that a square-based pyramid is

	4.10.7	Know and understand that a cone is a 3D shape with a circular base that tapers smoothly to a single vertex.	AO1
	4.10.8	Draw 3D shapes with straight edges and right angles using isometric grid paper.	AO2
	4.10.9	Know and understand that projections are 2D views of a 3D shape, including front elevation, side elevation, and plan view.	AO1
	4.10.10	Draw or sketch front, side, and top (plan) projections of 3D objects based on isometric drawings or given dimensions.	AO2
	4.10.11	Interpret projection (plan and elevation) drawings of 3D objects.	AO3
	4.10.12	Know and understand that a net is a 2D pattern that can be folded into a 3D solid.	AO1
	4.10.13	Sketch nets of common 3D shapes such as cubes, cuboids, pyramids, and prisms.	AO2
	4.10.14	Use the net of a 3D shape to calculate the total surface area of the shape by summing the areas of its faces.	AO3

Mensuration and Vectors

Aim: To break complicated systems down into simpler systems where sizes can be easily found.

	The learner will:	SLO#	Assessment Criteria - The learner can:	Cognitive levels
1	1 Understand how to find lengths, angles, perimeters and areas in 2D.	5.1.1	Measure line segments and angles accurately on scale drawings using a ruler and protractor.	AO2
		5.1.2	Interpret real-life maps and scale drawings by using measured lengths and angles.	AO3
		5.1.3	Construct straight lines and angles accurately on grid paper.	AO2
		5.1.4	Calculate the area of a triangle using the formula $Area = \frac{1}{2} \times (base \times height)$	AO2
		5.1.5	Calculate the areas of quadrilaterals using appropriate formulas: Parallelogram: base × height Kite: width × height Trapezium: ½ × (sum of parallel sides) × vertical height	AO2
		5.1.6	Calculate the circumference and area of a circle using $Circumference = 2\pi r = \pi d$ $Area = \pi r^2$	AO2
		5.1.7	Calculate arc length, sector area, and perimeter of a circular sector given the angle at the centre.	AO2
		5.1.8	Calculate the angle at the centre of a sector when given its arc length, perimeter, or area.	AO2
		5.1.9	Calculate the area and perimeter of composite 2D shapes by decomposing them into combinations of triangles, quadrilaterals, and sectors.	AO2
2	Understand how to find the surface areas and volumes of 3D shapes.	5.2.1	Calculate the surface area of cuboids, right prisms, regular tetrahedrons, and square-based pyramids.	AO2
	'	5.2.2	Calculate the surface area of a sphere using the formula $4\pi r^2$	AO2
		5.2.3	Calculate the surface area of a cone using the formula $A = \pi r l + \pi r^2$ where r is the base radius and l is the slant height (formula provided).	AO2
		5.2.4	Calculate the surface area of a cylinder using the formula $A = 2\pi r h + 2\pi r^2$ where r is the base radius and h is the height (formula provided).	AO2
		5.2.5	Calculate the surface area of related shapes, such as hemispheres or truncated cones, by adapting standard formulas.	AO2
		5.2.6	Calculate the volume of cuboids and right prisms using; Area of the front face × Depth of prism (Formula given)	AO2
		5.2.7	Calculate the volume of a sphere using the formula, $\frac{4}{3} \pi r^3$ there r is the radius (formula provided).	AO2
		5.2.8	Calculate the volume of a cone using and h is the height (formula provided). $v_{olume\ of\ the\ cone} = \frac{\bar{n}^2 k}{3}$ there r is the base radius	AO2
		5.2.9	Calculate the surface area and volume of composite 3D shapes by breaking them down into simpler standard solids.	AO2
		5.2.10	Use the properties of similar or congruent shapes in 2D and 3D to determine missing lengths, areas, or volumes.	AO2
3	Understand trigonometry.	5.3.1	Know and use the definitions of the trigonometric ratios for a right triangle: $\sin\theta = \text{Opposite/Hypotenuse},$ $\cos\theta = \text{Adjacent/Hypotenuse},$ $\tan\theta = \text{Opposite/Adjacent}.$	AO2
		5.3.2	Prove that $tan\theta = sin\theta / cos\theta$. (by trigonometric manipulation)	AO2
		5.3.3	Know and use the exact values of $\sin\theta$, $\cos\theta$ and $\tan\theta$ for the angles 0, 30, 45, 60 and 90 degrees, and explain why tan 90 is undefined.	AO2
		5.3.4	Use trigonometric functions to calculate unknown side lengths or angles in right-angled triangles.	AO2

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		5.3.5	Plot and sketch graphs of the trigonometric functions, $\sin\theta$, $\cos\theta$, and $\tan\theta$, where θ is any angle in degrees.	AO2
		5.3.6	Sketch the graphs of sin, cos and tan after the transformations 'Enlarge' ($A \ f \ (\theta \)$), 'Stretch' ($f \ (B \ \theta \)$), and/or '(Phase) Shift' ($f \ (\theta \ + C \)$).	AO2
		5.3.7	Use the 'Sine Rule' for finding unknown angles or side lengths of a general triangle, (equation give $\frac{a}{\sin A} - \frac{b}{\sin B} - \frac{c}{\sin C}$	AO2
		5.3.8	Use the 'Cosine Rule' for finding unknown angles or side lengths of a general triangle, (equation give $a^2 = b^2 + c^2 - 2bc \cos\theta$	AO2
		5.3.9	Use the area of a triangle sine rule, $Area = \frac{1}{2} ab \sin C$ to find the area, side lengths or angles of a general triangle (equation given).	AO2
		5.3.10	Prove the area of a triangle sine rule.	AO3
5.4	Understand vectors.	5.4.1	Identify scalar quantities as those with magnitude only (e.g. speed, distance, mass).	AO1
		5.4.2	Identify vector quantities as those with both magnitude and direction (e.g. velocity, displacement, force).	AO1
			Know and use vector notation, including row and column vectors, and the representations, \overrightarrow{oA} and \mathbf{v}	
		5.4.3	{Students should also be aware that in written rather than typed text there are other notations, $\bar{a}, \bar{b}, \text{or}\underline{c}$ Any clear and consistent notation in written answers will be accepted.}	AO1
		5.4.4	Know and understand how to multiply a vector by a scalar and interpret the result as a change in magnitude and/or direction.	AO1
		5.4.5	Know and understand how to add and subtract vectors numerically and algebraically, using component form.	AO1
		5.4.6	Express a given vector as a combination of other vectors when appropriate.	AO3
		5.4.7	Know and understand that the modulus (or magnitude) of a vector is its length and denote it as v .	AO1
		5.4.8	Calculate the modulus of a vector using Pythagoras' theorem in 2D.	AO2
		5.4.9	Draw vector diagrams, accurately labelling arrows to indicate direction and magnitude.	AO2
		5.4.10	Draw vectors on a grid, including those defined by magnitude and direction using bearings (e.g. "4 km at 065°").	AO2
		5.4.11	Interpret and analyze scale drawings and maps using bearings and vector directions.	AO3
		5.4.12	Know and understand the fact that translations can be represented by vectors.	AO1
		5.4.13	Use vectors to determine the image of a point after a translation in 2D.	AO2
		5.4.14	Apply vector methods to construct geometric arguments and simplify calculations.	AO3

Probability and Statistics

Aim: To calculate and interpret probabilities based on models of random events or data from experiments.

	The learner will:	SLO#	Assessment Criteria - The learner can:	Cognitive levels
1	Understand how probability applies to single events.	6.1.1	Know and understand an event is a describable situation where something may happen.	AO1
		6.1.2	Know and understand that an outcome is a possible result of an event, and the outcome as what actually occurs.	AO1
		6.1.3	Know and understand that a random event is one whose outcome cannot be predicted with certainty in advance.	AO1
		6.1.4	Know and understand that probability measures how likely an outcome is to occur and can be used to predict the likelihood of future events.	AO3
		6.1.5	Know and understand that probability values range between 0 (impossible) and 1 (certain), and can be expressed as fractions or decimals.	AO2
		6.1.6	Interpret values of 0 and 1 as representing certainty or impossibility.	AO2
		6.1.7	Demonstrate that no valid probability can be less than 0 or greater than 1.	AO3
		6.1.8	Know and use standard probability notation, e.g. P(Heads) = 0.5 or P(Red Card) = 26/52.	AO3
		6.1.9	Describe the likelihood of outcomes using qualitative labels and probability ranges:- "Definitely will happen" [P = 1] "Very likely" [P > 0.75] "Likely" [P > 0.5] "As likely as not" [P = 0.5] "Unlikely" [P < 0.5] "Very unlikely" [P < 0.25] "Definitely won't happen" [P = 0]	AO3
		6.1.10	Use and justify the rule: P(event happens) + P(event does not happen) = 1	AO2
		6.1.11	Show (by examples) that the sum of the probabilities of all possible outcomes of an event is always equal to 1.	AO2
		6.1.12	Know and understand "Equally Likely" outcomes as having the same probability, and describe such an event as fair.	AO1
		6.1.13	Identify events with unequal outcomes as biased or unfair.	AO1
		6.1.14	Know and use the formula for equally likely outcomes: $\frac{Number of wanted outcomes}{Total number of outcomes}$	AO2
		6.1.15	Apply probability reasoning to single-step events such as spinning a spinner, picking a card, or rolling a die.	AO2
2	Understand how probability applies to multiple events.	6.2.1	Know and understand mutually exclusive outcomes as outcomes where only one can occur at a time.	AO1
		6.2.2	Show that for an exhaustive set of mutually exclusive events, the sum of their probabilities is equal to 1.	AO3
		6.2.3	Use the rule that probabilities for all possible outcomes must sum to 1 to calculate missing probabilities.	AO2

		6.2.4	Recognize that in repeated experiments, relative frequency (outcome frequency ÷ total trials) estimates probability.	AO2
		6.2.5	Explain that small sample sizes may produce unreliable probability estimates, and that estimates improve with more trials.	AO3
		6.2.6	Use past relative frequency data to estimate the probability of a future event.	AO2
		6.2.7	Calculate expected frequency of an outcome using:(Understand this as an estimate, not a certainty.)	AO2
		6.2.8	Know and understand the sample space as the full list of possible outcomes for one or more events (e.g. sample space for two coin tosses = {HH, HT, TH, TT}).	AO1
		6.2.9	Identify independent events as events where one outcome does not influence the other.	AO1
		6.2.10	Identify dependent events as events where the outcome of one affects the outcome of the other.	AO1
		6.2.11	Know and apply the AND rule for independent events:P(A and B) = P(A) × P(B)	AO2
		6.2.12	Apply the OR rule for mutually exclusive events:P(A or B) = P(A) + P(B)	AO2
		6.2.13	Use listing techniques and the Product Rule for Counting to identify all possible outcomes of multiple-event experiments.	AO2
		6.2.14	Apply probability reasoning to multi-event contexts such as drawing multiple cards, rolling dice multiple times, or similar repeated random processes.	AO3
3	Understand how to use tables and diagrams to calculate probabilities of	6.3.1	Construct sample space diagrams (tables or grids) for two independent events to list all possible outcomes.	AO2
	multiple events.	6.3.2	Use sample space diagrams to calculate probabilities of specific combinations of outcomes, including mutually exclusive events.	AO3
		6.3.3	Draw and interpret Venn diagrams for two or more events, clearly labelling regions and sets.	AO2
		6.3.4	Use Venn diagrams to determine whether events are mutually exclusive or overlapping.	AO2
		6.3.5	Calculate the probability of an individual outcome or combined outcomes using set notation (e.g. $P(A \cup B)$, $P(A \cap B)$, $P(A')$).	AO2
		6.3.6	Use Venn diagrams to prove the OR rule for mutually exclusive events: $P(A \cup B) = P(A) + P(B)$	AO3
		6.3.7	Use Venn diagrams to calculate the probability that at least one of two non-mutually exclusive events occurs: $P(A \cup B) = P(A) + P(B) - P(A \cap B)$	AO2
		6.3.8	Draw and interpret tree diagrams for two or more sequential events.	AO2
		6.3.9	Know and use the rule that the probabilities on each branch at a node in a tree diagram must sum to 1, and that the total probability of all final outcomes is 1.	AO2
		6.3.10	Use diagrams (sample spaces, Venn, tree) to list and count all combinations in compound events.	AO2
		6.3.11	Calculate probabilities for combinations of events (independent, dependent, or mixed) using structured diagrams.	AO2
		6.3.12	State any assumptions made during probability calculations (e.g. events are independent or equally likely).	AO1
		6.3.13	Justify why assumptions made in probability models (e.g. fairness, independence) are valid or reasonable.	AO3

		6.3.14	Construct and interpret two-way tables to organize frequency or probability data across two categorical variables.	AO3
		6.3.15	Use expected frequencies or probability models (such as tree diagrams or two-way tables) to calculate and interpret conditional probabilities.	AO3
4	Understand how to collect data.	6.4.1	Know and understand the population as the entire group you want to study (e.g. all people at an event).	AO1
		6.4.2	Know and understand a member as an individual within a population.	AO1
		6.4.3	Know and understand a sample as a subset of members from the population used to represent the whole.	AO1
		6.4.4	Know and understand that a representative sample reflects the structure of the population and allows general conclusions.	AO2
		6.4.5	Know and understand a random sample as one where every member has an equal chance of being selected.	AO1
		6.4.6	Know and understand that representative samples should be both random and large enough to avoid bias.	AO1
		6.4.7	Identify a biased sample as one that over-represents or under-represents certain groups (e.g. only sampling men to represent all drivers).	AO3
		6.4.8	Know and understand that, as sample size increases, the results of repeated, unbiased sampling tend to match theoretical probability distributions.	AO1
		6.4.9	Identify flaws in sampling methods, such as poor selection criteria or insufficient size.	AO3
		6.4.10	Describe simple random sampling methods (e.g. number generators, drawing names from a hat).	AO2
		6.4.11	Describe and apply stratified sampling, where subgroups are proportionally represented in the sample.	AO2
		6.4.12	Use the results of a sample to infer properties of the whole population or distribution.	AO3
		6.4.13	Identify and explain limitations of sampling (e.g. small size, non-randomness, under-coverage).	AO3
		6.4.14	Recognize that effective surveys use clear, unbiased questions and response options that are easily recorded.	AO3
		6.4.15	Distinguish between qualitative data (descriptive, e.g. colors, opinions) and quantitative data (numerical).	AO3
		6.4.16	Classify quantitative data as either discrete (fixed values) or continuous (any value in a range), and organize them into "classes."	AO1
		6.4.17	Represent classes using equalities for discrete variables (e.g. "X = 3") and inequalities for continuous ones (e.g. "4 < X ≤ 6").	AO1
		6.4.18	Ensure that grouped data classes cover all possible responses (e.g. avoid missing "exactly 6 feet" in a height question).	AO2
		6.4.19	Explain flaws in questionnaires or how data was collected (e.g. leading questions, unclear categories, overlapping groups).	AO3
5	Understand how to process data.	6.5.1	Distinguish between the three types of average: mode, median, and mean.	AO1
		6.5.2	Know and understand the mode as the most frequent value in a data set; recognize when a data set is bimodal, trimodal, or multimodal.	AO1
		6.5.3	Know and understand that the median as the middle value in an ordered data set; for even-sized sets, calculate the average of the two central values.	AO1
	1		1	

		6.5.4	Calculate the mean by dividing the sum of all values by the number of values in the data set.	AO2
		6.5.5	Calculate and interpret the mean, median, and mode for given data sets.	AO2
		6.5.6	Evaluate the advantages and disadvantages of each average and select the most appropriate average for interpreting a given data set.	AO3
		6.5.7	Know and understand the range and interquartile range (IQR) as measures of data spread.	AO1
		6.5.8	Calculate the range as the difference between the highest and lowest values in the data set.	AO2
		6.5.9	Know and understand quartiles as values that divide an ordered set into four equal parts: - Q1 = 25% mark (lower quartile) - Q2 = 50% mark (median) - Q3 = 75% mark (upper quartile)	AO2
		6.5.10	Calculate the interquartile range as Q3 – Q1.	AO2
		6.5.11	Draw and interpret stem-and-leaf diagrams to determine quartiles and ranges.	AO2
		6.5.12	Draw and interpret box plots to represent quartiles, range, and IQR graphically.	AO2
		6.5.13	Draw and interpret frequency tables to find the mode, mean, and range for discrete data.	AO2
		6.5.14	Draw and interpret grouped frequency tables to identify modal and median classes and to estimate the mean and range for continuous data.	AO2
		6.5.15	Compare two data sets by analyzing their central tendency and spread, and comment on any outliers or anomalies that affect interpretation.	AO2
6	Understand statistical data graphs.	6.6.1	Draw and interpret common data representations, including tables, bar charts, pictograms, and pie charts.	AO2
		6.6.2	Construct and interpret cumulative frequency graphs to estimate quartiles and the interquartile range (IQR).	AO3
		6.6.3	Use cumulative frequency graphs to estimate the number of values above or below a given threshold.	AO3
		6.6.4	Construct histograms from grouped frequency tables using frequency density on the vertical axis.	AO2
		6.6.5	Use data from a histogram to complete a grouped frequency table.	AO2
		6.6.6	Draw frequency polygons using grouped data to visualize the distribution of values.	AO2
		6.6.7	Construct and complete two-way tables to represent relationships between two categorical or numerical variables.	AO2
		6.6.8	Plot scatter graphs from paired data sets and draw a line of best fit where appropriate.	AO3
		6.6.9	Use interpolation (within the data range) and extrapolation (beyond the data range) to make approximate predictions.	AO3
		6.6.10	Describe the risks and limitations of interpolation and especially extrapolation when interpreting trends.	AO3
		6.6.11	Know and understand that correlation as the relationship between two variables and explain that correlation does not imply causation.	AO1
		6.6.12	Know and understand correlation in terms of strength (strong, weak, none) and direction (positive, negative).	AO1

	6.6.13	Use scatter graphs to identify and justify correlation descriptions based on plotted data.	AO3
	nn 14	Draw conclusions and interpret key trends or features in a statistical data set using appropriate terminology.	AO3

FORMULA SHEET

Algebra

Compound interest = $P\left(1 + \frac{r}{100}\right)^n$ n^{th} term of Arithmetic sequence $(a_n) = a_1 + (n-1)d$ n^{th} term of Geometric sequence $(a_n) = a_1r^{n-1}$ n^{th} term of Triangular sequence $(a_n) = n \times \frac{(n+1)}{2}$ n^{th} term of Quadratic sequence $(a_n) = an^2 + bn + c$ Quadratic Formula: $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

Kinematics

$$s = ut + \frac{1}{2}at^{2}$$

$$v = u + at$$

$$v^{2} = u^{2} + 2as$$

Geometry

 $Area\ of\ a\ triangle = \frac{1}{2}\times(base\ \times height)$ $Area\ of\ a\ parallelogram = base\ \times height$ $Area\ of\ a\ Kite = base\ \times height$ $Area\ of\ a\ Circle = 2\pi r = \pi d$ $Area\ of\ a\ circle = 2\pi r = \pi d$ $Area\ of\ a\ circle = \pi r^2$ $Surface\ Area\ of\ a\ Sphere = \pi r^2$ $Surface\ Area\ of\ a\ Cone = \pi rl + \pi r^2$ $Surface\ Area\ of\ a\ Colinder = 2\pi rh + 2\pi r^2$ $Volume\ of\ the\ sphere = \frac{4}{3}\pi r^3$ $Volume\ of\ the\ cone = \frac{\pi r^2 h}{3}$ $Cosine\ rule: a^2 = b^2 + c^2 - 2bc\ cos\theta$ $Area\ of\ a\ triangle\ sine\ rule = \frac{1}{2}ab\ sinC$